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OPEN Application of multi-extruded fuel injectors for mixing enhancement of hydrogen gas at scramjet engine: computational study

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Scramjet engines are considered a highly promising technology for improving high-speed flight. In this study, we investigate the effects of using multi-extruded nozzles on fuel mixing and distribution inside the combustion chamber at supersonic flow. Additionally, we explore the impact of an inner air jet on fuel mixing in annular nozzles. To model fuel penetration in the combustor, we employ a computational technique. Our study compares the roles of three different extruded injectors on fuel diffusion and distribution at supersonic cross-flow. Our findings reveal that the use of an inner air jet increases fuel mixing in the annular jet, while the use of extruded nozzles improves fuel distribution by enhancing the vortices between injectors. These results demonstrate the potential benefits of incorporating multi-extruded nozzles and inner air jets in the design of scramjet engines.

The development of scramjet engines has received considerable attention in recent years due to their potential to improve high-speed flight¹⁻³. One of the key challenges in designing these engines is achieving efficient fuel mixing and distribution at supersonic flow within the combustion chamber. In this context, the present study investigates the use of multi extruded nozzles to enhance fuel mixing and distribution. The study also explores the impact of an inner air jet on fuel mixing in annular nozzles. The computational modeling technique is employed to analyze the fuel penetration and diffusion in the combustor^{4,5}. The study compares the performance of three different extruded injectors in terms of fuel diffusion and distribution at supersonic cross flow. The findings reveal that the use of extruded nozzles and inner air jet can significantly improve fuel mixing and distribution by enhancing the vortices between injectors. The results of this study have important implications for the design and development of more efficient and effective scramjet engines⁶⁻⁸.

Scramjet engines have been a topic of extensive research due to their potential to achieve high-speed flight and space access⁹⁻¹¹. The critical challenge in designing these engines is to achieve efficient fuel mixing and distribution, as the combustion process is highly sensitive to these factors¹²⁻¹⁴. One way to improve fuel mixing and distribution is by using multi-nozzle injectors. A study¹⁵ investigated the use of multi-jet injectors in a Mach 6 scramjet combustor and found that the use of multi-jet injectors improved the combustion efficiency and reduced the flame length.

Another approach to improve fuel mixing and distribution is by using transverse injection, where fuel is injected perpendicular to the air flow. Several studies^{4,16,17} investigated the use of transverse injection in a Mach 4 scramjet engine and found that it significantly improved fuel mixing and distribution.

The use of swirling flow to enhance fuel mixing and distribution has also been explored. Many papers¹⁸⁻²¹ investigated the use of swirling flow in a Mach 2.5 scramjet engine and found that it improved fuel mixing and distribution by promoting turbulence and increasing residence time. The impact of fuel injection pressure on fuel mixing and distribution has also been studied. Many papers^{22–26} investigated the effect of fuel injection pressure on the combustion efficiency of a Mach 3 scramjet engine and found that higher injection pressures improved fuel mixing and distribution, resulting in higher combustion efficiency.

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The impact of nozzle shape and geometry on fuel mixing and distribution has also been explored. Many papers^{26–29} investigated the effect of nozzle geometry on the combustion efficiency of a Mach 5 scramjet engine and found that the use of lobed injectors improved fuel mixing and distribution compared to circular injectors.

In summary, there have been various approaches to improving fuel mixing and distribution in scramjet engines, including the use of multi-nozzle injectors, transverse injection, swirling flow, higher injection pressures, and optimized nozzle geometry³⁰⁻³³. These studies provide valuable insights for the design and development of more efficient and effective scramjet engines³⁴⁻³⁶.

This study has tried to investigate the influence of different arrangements of extruded lobe-injectors on the fuel penetration and shock interactions inside the combustion chamber. To do this, shock waves are compared on the jet planes to reveals the influence of extruded configurations on the fuel mixing mechanism at supersonic flow. Various lobe nozzles are investigated as demonstrated in Fig. 1. The effects of both annular and coaxial fuel and air jet are fully investigated in this research.

Governing equations and numerical methodology

The simulation of high-speed air stream with compressibility effects is mainly done via solving RANS equations for continuum domain^{37–40}. The shock wave formation is inherently happened in our model and consequently, the energy equation must be considered in our modeling^{41,42}. Meanwhile, the turbulence effects are also important in our model and SST model of turbulence is considered for the calculation of viscosity^{31,42,43}. The secondary gas of hydrogen is also modeled as fuel jet and mass transport equation is also used with Fick. Law for estimation of the diffusion of hydrogen gas^{44,45}. Reactions are not considered in this study. The air flow is considered as ideal gas in the present model^{46–51}.

Figure 1 illustrates the shape of the injector and arrangement of the nozzle inside the model. The fuel jet is injected through annular nozzle while air jet is released from inner core of the nozzle. The size of outer and inner nozzle is equal and equivalent to circular nozzle with diameter of 0.5 mm. The jet distance of these injector in all configurations is 3.5 mm and the height of extruded nozzle of 2nd, 3rd and 4th nozzle is 0.5 mm, 1 mm and 1.5 mm. The length, width and height of computational domain are 80 mm, 5 mm and 6 mm, respectively. At inlet, air stream with Mach number of 4 and static temperature of 1000 K is applied. The fuel and air jets are released with Mach = 1 and 10% total pressure of supersonic air stream. Half of real model is simulated to reduce the computational $cost^{52}$. The usage of theoretical method is conventional in engineering applications⁵³⁻⁵⁶.

The produced grid for the selected computational domain is displayed in Fig. 2. The structured grid is applied for the model because of the shock interactions. Besides, the resolution of generated grid must be high enough in the regions nearby the nozzle since these districts are potential for the high velocity and density gradient. The grid study is also done to obtain the proper size of grid for the present investigations. Table 1 presents the results of grid independency analysis and it is noticed that the fine grid is most efficient grid for the chosen model.

Results and discussion

The correctness of the achieved data from the computational study is evaluated to certify the precision of the applied approach. Figure 3 displayed the value of fuel penetration of single circular nozzle with diameter of 2 mm at supersonic flow. These outcomes advocate that the single-jet numerical solution is accurate in terms of the penetration downstream of jet³⁸ (Table 2).



Figure 1. Problem description.



Figure 2. Grid production.

	Cells	Grid cells. along X, Y and Z direction	Hydrogen fraction at 30 mm downstream
Coarse	943,100	176×114×50	0.292
Medium	1,610,100	196×144×60	0.301
Fine	2,223,100	218×170×70	0.307
Very fine	3,800,100	242×200×80	0.308

Table 1. Grid study.

Figure 3a illustrates the primary feature of shock waves layer near these annular injectors at supersonic flow on the symmetry plane. The Mach contour of the proposed configuration reveals that the shear layer and jet bow shack significantly varies by the shape of injector on the jet plane. Indeed, the jet bow shock, which is produced by the velocity of fuel jet, deformed by the incoming air stream. When the simple injectors are used, the growth of shear layer is related to the total pressure of jet and free stream condition. However, in extruded jet configuration, the jet plume is related to the height of extruded nozzles. The difference of the shock layer for the model with inner air jet (Fig. 3b) with former annular cases (Fig. 3a) indicates that the high pressure of the coaxial fuel and air jet released from the extruded nozzle results separation shock upstream of the first nozzle. Hence, the formation of the barrel fuel jet is not changed under influence of the incoming supersonic flow.

Figure 4a illustrates the contour of mass on the symmetry plane for different annular lobe-nozzles. When the extruded injector is applied for the fuel mixing, the height of the fuel mixing zone is managed by the height of the extruded injectors. As confirmed by the mass contour, the concentration of the fuel jet and penetration height is directly varied by the nozzle height. Besides, the interactions of the fuel jet with main stream almost constant for all jets. In fact, the main advantageous of this concept is management of the fuel diffusion and the efficient fuel diffusion by the jet interactions even in last injectors. As depicted in Fig. 4b, the addition of inner air jet also has meaningful impacts on the concentration and diffusion of the fuel jet in proposed configurations. Comparison of coaxial nozzle with annular one shows that the usage of inner air flow substantially improves the circulation in the gap of injector which enhance the fuel mixing and diffusion of the fuel in the depth of the domain. Indeed, the fuel mixing is more efficient in this configuration.

The three-dimensional flow feature of annular jet configurations (Fig. 5a) disclosed the influence of the circulation in the gap of the injectors on the jet layer at supersonic flow. The comparison of different lobe-nozzle types shows that the fuel distribution inside the main stream is improved by the nozzle with 4-lobe shape. In facts, the fuel jet released from wider area in 4-lobe nozzles and this extend the fuel plume inside the combustion chamber. The injection of the air jet in the recommended jet arrangements (Fig. 5b) shows that the jet interactions are extremely amplified when inner air jet is coupled with annular fuel jets. Meanwhile, the effects of the upstream circulation on the distribution of the fuel jet is more pronounced in the coaxial air and fuel injection.

In Fig. 6, the jet stream along with fuel jet is investigated and displayed to reveal the importance of jet interactions on the mechanism of fuel diffusion in combustion chamber for the proposed models. As mentioned in the previous sections, the interactions of the air and fuel jet becomes extraordinary when extruded multi-nozzles is used in supersonic flow. As demonstrated in Fig. 6a, each jet has its own interactions with air stream in the



Figure 3. Comparison of Mach contour for (a) annular jet system (b) coaxial jet.

Distance from injector (mm)	Our data	Numerical data of Fallah ¹¹	Errors (%)
5	5.68	6.3	10
10	7.05	7.5	6
20	8.05	7.7	4.5
30	8.35	8.5	2.5

Table 2. penetration height (mm).

extruded configurations and the formation of the vortex within the gap of extruded nozzle is extended by the height of the fuel nozzle. These two features are considerably important for the distribution of the fuel multi-jets. As illustrated for the coaxial jet configurations (Fig. 6b), higher jet interactions are achieved by adding inner air jet and this extend the upstream circulations. Therefore, horseshoe vortex with stronger circulation extend to downstream. As the normal momentum of the fuel and air jets increases in this model, the pressure in the gap of nozzle is extended and this enables the formation of the vortex in this region. Therefore, the fuel distribution is more uniform in this configuration.

Comparison of the mixing zone and stream feature on two planes (x/D = 10 and 30) down stream of three suggested nozzle configurations are done in Fig. 7. In the vicinity of nozzle (Fig. 7a), the height of fuel penetration is less for annular injector while higher fuel penetration is noticed for the coaxial model. There are two main vortices behind the jet and strength and size of these vortices clearly disclose the role of injector type and existence of inner air jet in the planned configurations. The main circulations (Vortex A) is inherently produced by the normal velocity of fuel jet and second one (Vortex B) is related to the horseshoe vortex. In some nozzle the secondary vortex is not observed especially in the coaxial model. In the far distance (Fig. 7b), the position of these two vortices are changed and the concentration of the fuel gas becomes uniform by the usage of inner air jet.

Comparison of the circulation strength downstream of the proposed configurations is presented in Fig. 8. The variation of the circulation power indicates that replacing the annular jet with coaxial air and fuel jet decreases the circulation power in all models. Among these injector types, 3-lobe model has maximum circulation power and this is due to the formation of larger upstream circulation. The data of circulation shows that the impacts of injector types and nozzle is almost in range of 10 mm to 20 mm behind the first nozzle.

Figure 9 plots the changes of fuel mixing behind the fuel nozzles for the proposed extruded injectors. The mixing efficiency of coaxial air and fuel jet is almost 44% more than annular nozzle. The main performance of injector type is noticed near the injectors. In the coaxial nozzle configurations, the 3-lobe nozzle performs more efficient in fuel distribution than other injector configurations.

Conclusion

This study focuses on investigating the effects of multi extruded injectors on the fuel mixing mechanism in scramjet engines. Specifically, we examine the roles of three different types of nozzles located inside the engine's combustor, including annular and coaxial nozzles. To model the release of fuel jet from the extruded nozzles at supersonic cross flow, we develop a computational fluid dynamic approach. Through this approach, we compare the mixing efficiency and circulation power of each model. Our findings indicate that the use of coaxial jet nozzles decreases the circulation power, while achieving maximum fuel mixing efficiency. Additionally, we observe that the utilization of an inner air jet in the coaxial configuration further enhances fuel mixing in the nozzle gap.



Figure 4. Comparison of flow stream and fuel concentration on the symmetry plane for (**a**) annular jet system (**b**) coaxial jet.



b)



Figure 5. Comparison of three-dimensional flow near the extruded nozzle for (**a**) annular jet system (**b**) coaxial jets.



Figure 6. Comparison of flow and jet interactions for (a) annular jets (b) coaxial jets system.

a)



Figure 7. Comparison of mass concentration and stream of annular and coaxial jets at (**a**) X/D = 10, (**b**) X/D = 30 downstream of first jet.



Figure 8. Comparison of the circulation induced by jet type downstream of the injectors.



Figure 9. Comparison of the fuel mixing efficiency downstream of the injectors.

Data availability

All data generated or analysed during this study are included in this published article.

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References

- 1. Choubey, G., & Tiwari, M. Scramjet combustion: Fundamentals and advances (Butterworth-Heinemann, 2022).
- 2. Choubey, G., Solanki, M., Patel, Om., Devarajan, Y. & Huang, W. Effect of different strut design on the mixing performance of H2 fueled two-strut based scramjet combustor. *Fuel* **351**, 128972 (2023).
- 3. Barzegar Gerdroodbary, M. Aerodynamic heating in supersonic and hypersonic flows: Advanced techniques for drag and aeroheating reduction (Elsevier, 2022).
- 4. Wang, S.-y, Zhao-bo, Du., Huang, W. & Choubey, G. Numerical study on a novel device for hydrogen mixing enhancement in a scramjet engine: Coaxial injector. *Aerosp. Sci. Technol.* **127**, 107680 (2022).
- 5. Faress, F. *et al.* Phase equilibria simulation of biomaterial-hydrogen binary systems using a simple empirical correlation. *Processes* **11**(3), 714 (2023).
- 6. Gerdroodbary, M. B. Scramjets: Fuel mixing and injection systems, pp. 1-220 (Elsevier Ltd., Oxford, UK, 2020).
- Hassanvand, A., Gerdroodbary, M. B. & Abazari, A. M. Injection of hydrogen sonic multi-jet on inclined surface at supersonic flow. Int. J. Mod. Phys. C (IJMPC) 32(03), 1–14 (2021).

- Choubey, G., Yuvarajan, D., Huang, W., Shafee, A. & Pandey, K. M. Recent research progress on transverse injection technique for scramjet applications-a brief review. *Int. J. Hydrogen Energy* 45(51), 27806–27827 (2020).
- 9. Hassanvand, A., Moghaddam, M. S., Gerdroodbary, M. B. & Amini, Y. Analytical study of heat and mass transfer in axisymmetric unsteady flow by ADM. *JCARME* 11(1), 151–163 (2021).
- Jiang, Y., Hajivand, M., Sadeghi, H., Gerdroodbary, M. B. & Li, Z. Influence of trapezoidal lobe strut on fuel mixing and combustion in supersonic combustion chamber. Aerosp. Sci. Technol. 1, 106841 (2021).
- 11. Fallah, K., Gerdroodbary, M. B., Ghaderi, A. & Alinejad, J. The influence of micro air jets on mixing augmentation of fuel in cavity flameholder at supersonic flow. *Aerosp. Sci. Technol.* **76**, 187–193 (2018).
- Choubey, G. & Pandey, K. M. Effect of parametric variation of strut layout and position on the performance of a typical two-strut based scramjet combustor. *Int. J. Hydrogen Energy* 42(15), 10485–10500 (2017).
- Sun, C., Gerdroodbary, M. B., Abazari, A. M., Hosseini, S. & Li, Z. Mixing efficiency of hydrogen multijet through backward-facing steps at supersonic flow. *Int. J. Hydrogen Energy* 1, 1 (2021).
- Li, Z., Gerdroodbary, M. B., Moradi, R., Manh, T. D. & Babazadeh, H. Effect of inclined block on fuel mixing of multi hydrogen jets in scramjet engine. *Aerosp. Sci. Technol.* 105, 106035. https://doi.org/10.1016/j.ast.2020.106035 (2020).
- 15. Choubey, G. et al. Recent advances in cavity-based scramjet engine-a brief review. Int. J. Hydrogen Energy 44(26), 13895–13909 (2019).
- Gerdroodbary, M. B. & Hosseinalipour, S. M. Numerical simulation of hypersonic flow over highly blunted cones with spike. Acta Astronaut. 67(1–2), 180–193 (2010).
- Jiang, Y., Gerdroodbary, M. B., Sheikholeslami, M., Babazadeh, H., Shafee, A., Moradi, R., Li, Z. Effect of free stream angle on mixing performance of hydrogen multi-jets in supersonic combustion chamber. Int. J. Hydrogen Energy. https://doi.org/10.1016/j. ijhydene.2020.06.055 (2020).
- 18. Shang, S. et al. The impact of inner air jet on fuel mixing mechanism and mass diffusion of single annular extruded nozzle at supersonic combustion chamber. Int. Commun. Heat Mass Transfer 146, 106869 (2023).
- Far, S. B. et al. Optimizing the amount of concentration and temperature of substances undergoing chemical reaction using response surface methodology. Int. J. Thermofluids 17, 100270 (2023).
- Pish, F., Hassanvand, A., Gerdroodbary, M. B. & Noori, S. Viscous equilibrium analysis of heat transfer on blunted cone at hypersonic flow. *Case Stud. Therm. Eng.* 14, 100464 (2019).
- 21. Li, Y., Zhu, G., Chao, Y., Chen, L. & Alizadeh, A. Comparison of the different shapes of extruded annular nozzle on the fuel mixing of the hydrogen jet at supersonic combustion chamber. *Energy* 12, 8142 (2023).
- Li, Z. et al. Computational investigation of multi-cavity fuel injection on hydrogen mixing at supersonic combustion chamber. Int. J. Hydrogen Energy 45(15), 9077–9087 (2020).
- 23. Zhang, Y., Gerdroodbary, M. B., Hosseini, S., Abazari, A. M. & Li, Z. Effect of hybrid coaxial air and hydrogen jets on fuel mixing at supersonic crossflow. *Int. J. Hydrogen Energy* 1, 1 (2021).
- 24. Pish, F. et al. Computational study of the cavity flow over sharp nose cone in supersonic flow. Int. J. Mod. Phys. C 20, 50079 (2020).
- Ma, L., Liu, X., Liu, H., Alizadeh, A. & Shamsborhan, M. The influence of the struts on mass diffusion system of lateral hydrogen micro jet in combustor of scramjet engine: Numerical study. *Energy* 12, 8119 (2023).
- 26. Shi, X. *et al.* Influence of coaxial fuel-air jets on mixing performance of extruded nozzle at supersonic combustion chamber: Numerical study. *Phys. Fluids* **35**(5), 1 (2023).
- 27. Shi, Y. *et al.* Influence of lateral single jets for thermal protection of reentry nose cone with multi-row disk spike at hypersonic flow: Computational study. *Sci. Rep.* **13**(1), 6549 (2023).
- Gerdroodbary, M. B., Fallah, K. & Pourmirzaagha, H. Characteristics of transverse hydrogen jet in presence of multi air jets within scramjet combustor. Acta Astronaut. 132, 25–32 (2017).
- 29. Li, Y. *et al.* Three-dimensional DSMC simulation of thermal Knudsen force in micro gas actuator for mass analysis of gas mixture. *Measurement* 1, 107848 (2020).
- Sheidani, A., Salavatidezfouli, S. & Schito, P. Study on the effect of raindrops on the dynamic stall of a NACA-0012 airfoil. J. Braz. Soc. Mech. Sci. Eng. 44(5), 1–15 (2022).
- Iranmanesh, R., Alizadeh, A., Faraji, M. & Choubey, G. Numerical investigation of compressible flow around nose cone with multi-row disk and multi coolant jets. Sci. Rep. 13(1), 787 (2023).
- Li, S., Mao, L., Alizadeh, A., Zhang, X. & Valiallah Mousavi, S. The application of non-uniform magnetic field for thermal enhancement of the nanofluid flow inside the U-turn pipe at solar collectors. *Sci. Rep.* 13(1), 8471 (2023).
- 33. Edalatpour, A., Hassanvand, A., Barzegar Gerdroodbary, M., Moradi, R. & Amini, Y. Injection of multi hydrogen jets within cavity flameholder at supersonic flow. *Int. J. Hydrogen Energy* **44**(26), 13923–13931 (2019).
- Barzegar Gerdroodbary, M., Moradi, R. & Babazadeh, H. Computational investigation of multi hydrogen jets at inclined supersonic flow. Int. J. Energy Res. 1, 1. https://doi.org/10.1002/er.5821 (2020).
- Fallah, K., Fardad, A. & Fattahi, E. Numerical simulation of planar shear flow passing a rotating cylinder at low Reynolds numbers. Acta Mech. 223(2), 221–236 (2012).
- Fallah, K., Rahni, M. T., Mohammadzadeh, A. & Najafi, M. Drop formation in cross-junction micro-channel using lattice Boltzmann method. *Therm. Sci.* 22(2), 909–919 (2018).
- Abdollahi, S. A., Rajabikhorasani, G. & Alizadeh, A. Influence of extruded injector nozzle on fuel mixing and mass diffusion of multi fuel jets in the supersonic cross flow: computational study. *Sci. Rep.* 13, 12095. https://doi.org/10.1038/s41598-023-39306-z (2023).
- Gerdroodbary, M. B. Numerical analysis on cooling performance of counterflowing jet over aerodisked blunt body. Shock Waves 24(5), 537–543 (2014).
- Moradi, R., Mahyari, A., Barzegar Gerdroodbary, M., Abdollahi, A. & Amini, Y. Shape effect of cavity flameholder on mixing zone of hydrogen jet at supersonic flow. *Int. J. Hydrogen Energy* 43(33), 16364–16372 (2018).
- Anazadehsayed, A., Barzegar Gerdroodbary, M., Amini, Y. & Moradi, R. Mixing augmentation of transverse hydrogen jet by injection of micro air jets in supersonic crossflow. Acta Astronaut. 137, 403–414 (2017).
- Moradi, R., Mosavat, M., Barzegar Gerdroodbary, M., Abdollahi, A., & Amini, Y. The influence of coolant jet direction on heat reduction on the nose cone with Aerodome at supersonic flow. Acta Astronaut. 151, 487–493 (2018).
- Pudsey, A. S. & Boyce, R. R. Numerical investigation of transverse jets through multiport injector arrays in a supersonic crossflow. J. Propul. Power 26(6), 1225–1236 (2010).
- Cheng, Z., Guo, Z., Fu, P., Yang, J. & Wang, Q. New insights into the effects of methane and oxygen on heat/mass transfer in reactive porous media. Int. Commun. Heat Mass Transfer 129, 105652. https://doi.org/10.1016/j.icheatmasstransfer.2021.105652 (2021).
- Wang, H., Wu, X., Zheng, X. & Yuan, X. model predictive current control of nine-phase open-end winding PMSMS with an online virtual vector synthesis strategy. *IEEE Trans. Ind. Electron.* 1, 1. https://doi.org/10.1109/TIE.2022.3174241 (2022).
- Bai, X., He, Y. & Xu, M. Low-thrust reconfiguration strategy and optimization for formation flying using Jordan normal form. IEEE Trans. Aerosp. Electron. Syst. 57(5), 3279–3295. https://doi.org/10.1109/TAES.2021.3074204 (2021).
- Liu, L., Peng, Y., Zhang, W. & Ma, X. Concept of rapid and controllable combustion for high power-density diesel engines. *Energy Convers. Manag.* 276, 116529. https://doi.org/10.1016/j.enconman.2022.116529 (2023).
- Shen, D., Cheng, M., Wu, K., Sheng, Z. & Wang, J. Effects of supersonic nozzle guide vanes on the performance and flow structures of a rotating detonation combustor. *Acta Astronaut.* 193, 90–99. https://doi.org/10.1016/j.actaastro.2022.01.002 (2022).

- Wu, Y., Liu, L., Liu, B., Cao, E. & Xiong, Q. Investigation of rapid flame front controlled knock combustion and its suppression in natural gas dual-fuel marine engine. *Energy* 279, 128078. https://doi.org/10.1016/j.energy.2023.128078 (2023).
- Bai, X., Huang, M., Xu, M. & Liu, J. Reconfiguration optimization of relative motion between elliptical orbits using Lyapunov-Floquet transformation. *IEEE Trans. Aerosp. Electron. Syst.* 59(2), 923–936. https://doi.org/10.1109/TAES.2022.3193089 (2023).
- Liu, L., Fu, S. & Han, C. Investigation on diesel spray flame evolution and its conceptual model for large nozzle and high-density of ambient gas. *Fuel* **339**, 127357. https://doi.org/10.1016/j.fuel.2022.127357 (2023).
- Kun, Z. et al. Analysis of Lower Cambrian shale gas composition, source and accumulation pattern in different tectonic backgrounds: A case study of Weiyuan Block in the Upper Yangtze region and Xiuwu Basin in the Lower Yangtze region. Fuel 263, 115978. https://doi.org/10.1016/j.fuel.2019.115978 (2020).
- 52. Sheidani, A., Salavatidezfouli, S., Stabile, G., Gerdroodbary, M. B., & Rozza, G. Assessment of icing effects on the wake shed behind a vertical axis wind turbine. *Phys. Fluids* **35**(9) (2023).
- Khani, S., Haghighi, S. S., Razfar, M. R., & Farahnakian, M. Optimization of dimensional accuracy in threading process using solid-lubricant embedded textured tools. *Mater. Manuf. Process.* 37(3), 294–304 (2022).
- Farahnakian, M., S. Elhami, H. Daneshpajooh, and M. R. Razfar. Mechanistic modeling of cutting forces and tool flank wear in the thermally enhanced turning of hardened steel. *Int. J. Adv. Manuf. Technol.* 88, 2969–2983 (2017).
- Farahnakian, M., Keshavarz, M. E., Elhami, S., & Razfar, M. R. Effect of cutting edge modification on the tool flank wear in ultrasonically assisted turning of hardened steel. Proc. Inst. Mech. Eng. Part B J. Eng. Manuf. 233(5), 1472–1482 (2019).
- Farahnakian, M., Razfar, M. R. & Biglari, F. R. Multi-constrained optimization in ultrasonic-assisted turning of hardened steel by electromagnetism-like algorithm. *Proc Inst Mech Eng B J Eng Manuf* 229 (11), 1933–1944 (2015).

Author contributions

S.A.A. and S.F.R. wrote the main manuscript text, and S. A. and M.F. prepared figures P.D.U. supervised project. All authors reviewed the manuscript.

Competing interests

The authors declare no competing interests.

Additional information

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