



Structural Equation Modeling

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Objective of Presentation

- ✓ To gain acquaintance about the basics of Structural Equation Modeling.



Introduction

- ✓ SEM is a multivariate statistical analysis technique that is used to analyze structural relationships.
- ✓ SEM is the combination of factor analysis and multiple regression analysis.
- ✓ SEM is used to analyze the structural relationship between measured variables and latent variables.



Introduction

- ✓ SEM is preferred by the researcher because it estimates the multiple and interrelated dependence in a single analysis.
- ✓ SEM enables the researcher to include unobservable variables which were measured indirectly by the variables and facilitates error term attached to the observed variable.
- ✓ In this analysis, two types of variables are used: Endogenous variables and Exogenous variables.



Exogenous & Endogenous Variables

1. Exogenous variables

- assumed to be external to the model
- no other variable points at it in a model
- independent variables
- constitutes the periphery of the model

2. Endogenous variables

- predicted by other variables in the model
- directed arrow entering into them in a model
- dependent variables on one or more variables
- constitutes the inner core of the model



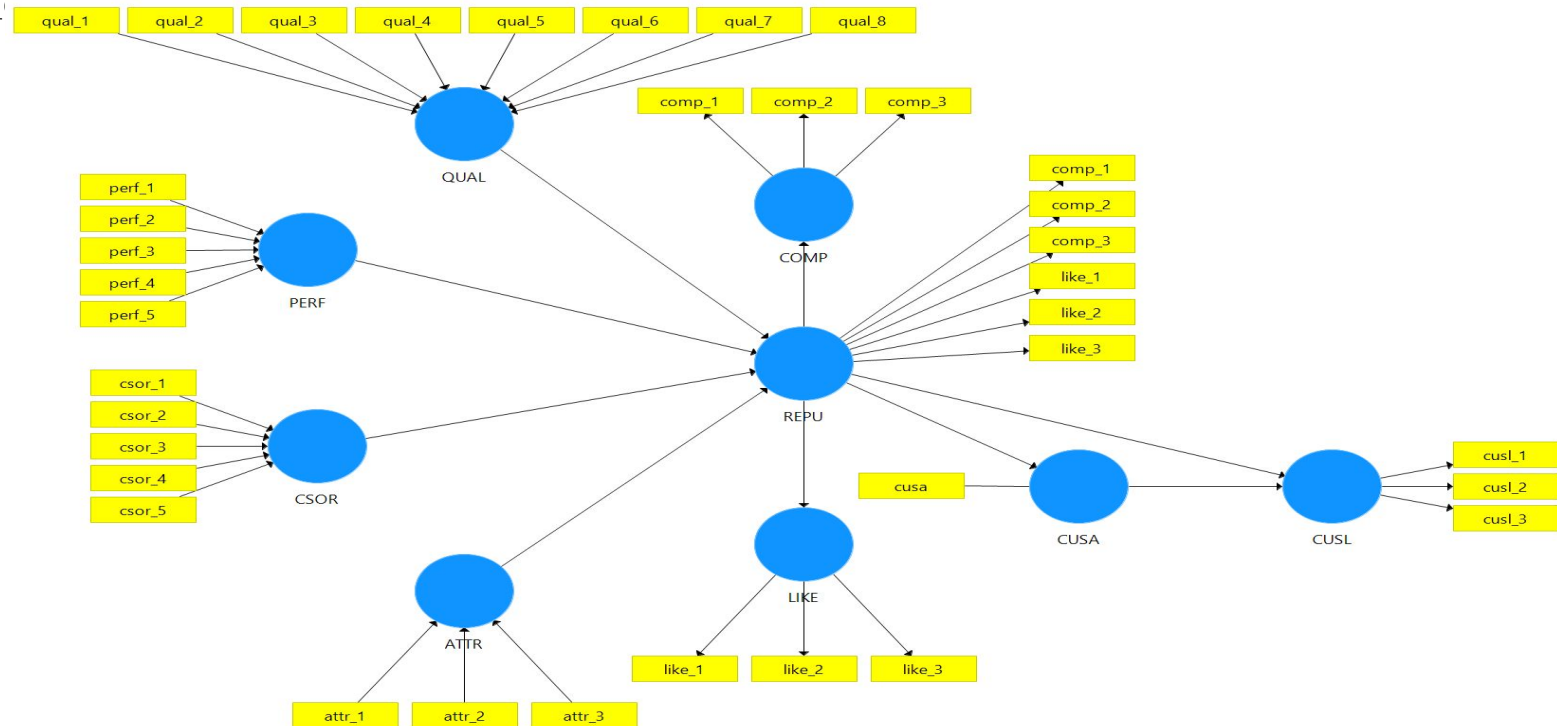
Types of Constructs in a Model

- 1. Observed Variables:** are called as Indicators. (items or observed variables in SPSS & AMOS). Directly measured in SEM.
- 2. Latent Variables/Constructs:** are abstract, not measured directly in SEM and represent the group of indicators.



Order of Constructs

1. First Order Construct: Outer tier of latent variables / exogenous variables which are immediately attached with the indicators

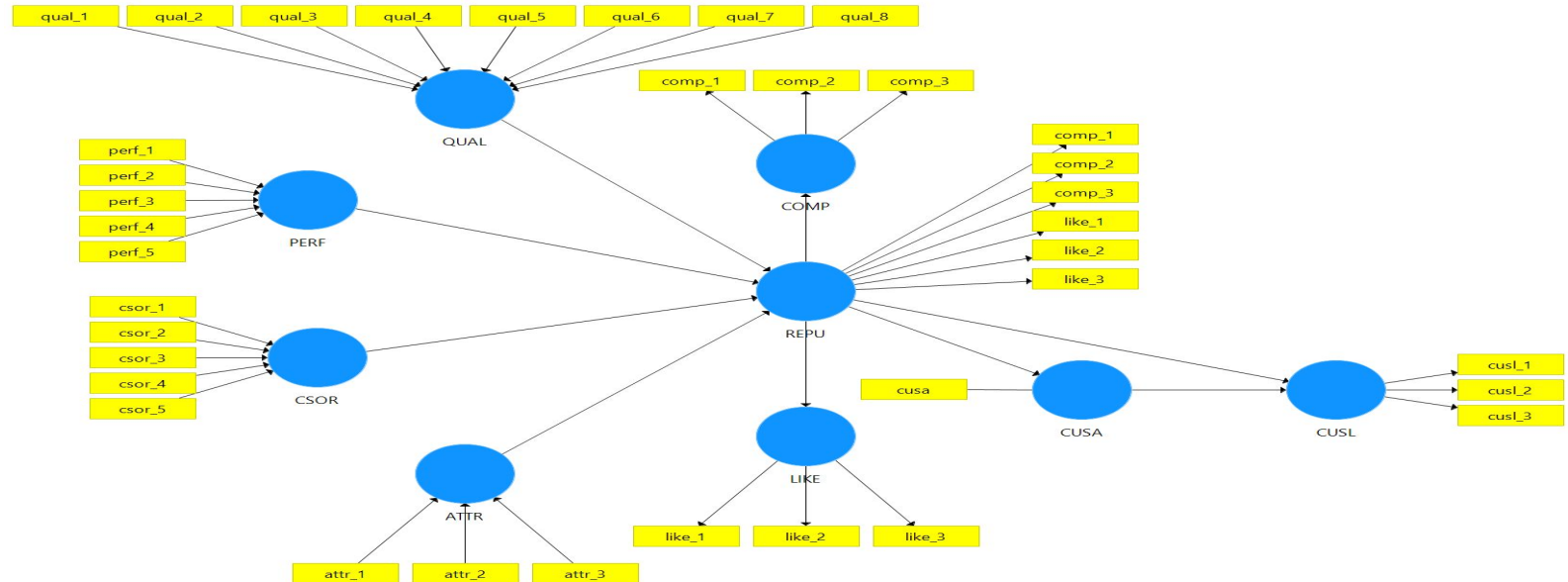




Order of Constructs

2. Second Order Constructs or Higher Order Constructs:

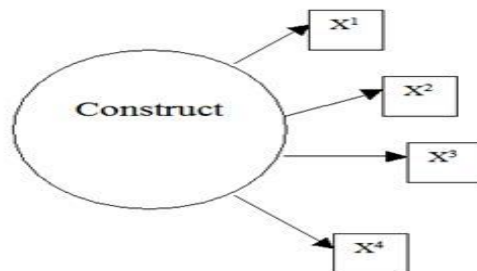
Constructs attached with the First Order Constructs are called Second Order Constructs.



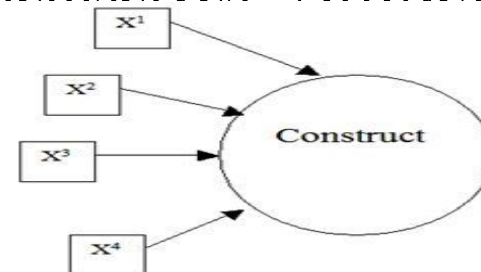
Types of Models

1. Reflective Models: If the indicators are caused by the latent construct and interchangeable among themselves. Multiple indicators direct outwards with their arrows directed from latent constructs to indicators.

2. Formative Models: If the indicators cause the latent construct and are not interchangeable among themselves. Arrows direct inwards from



Reflective



Formative

Summary



SEM model components

Exogenous construct (a.k.a. independent construct)

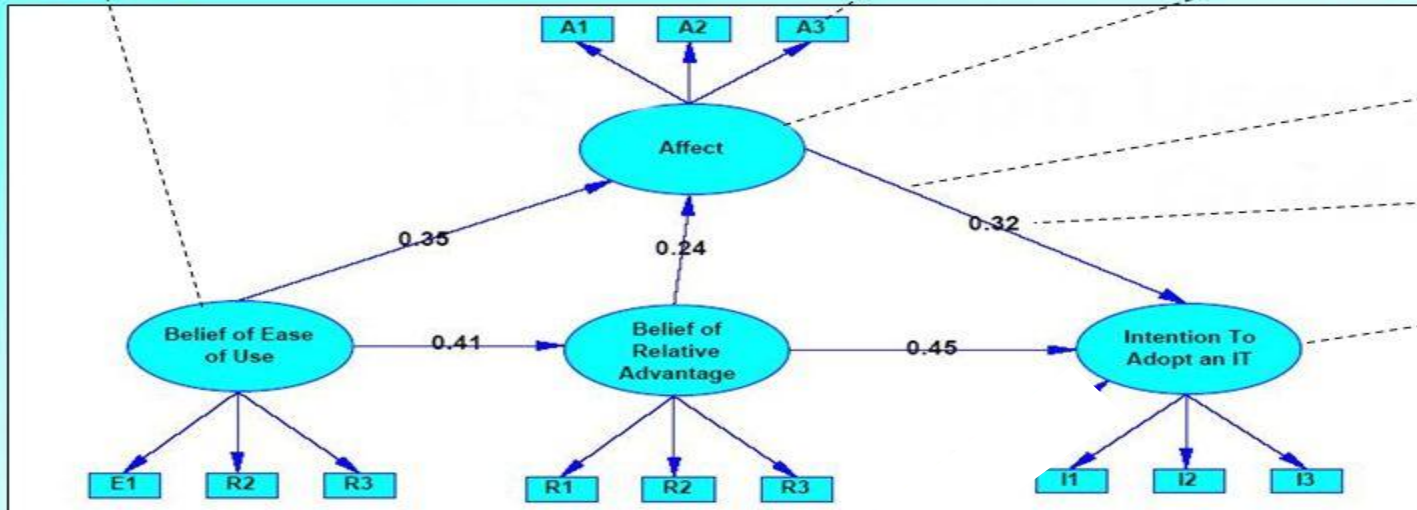
Indicator

Construct (a.k.a. latent variable)

Path

Path coefficient

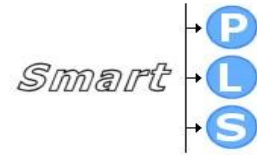
Endogenous construct (a.k.a. dependent construct)





SEM Softwares in Market

1. SmartPLS



2. R program



3. Lavaan (Latent Variable Analysis)

```
library(lavaan)

model <- '
# latent variables
ind60 =~ x1 + x2 + x3
dem60 =~ y1 + y2 + y3 + y4
dem65 =~ y5 + y6 + y7 + y8
# regressions
dem60 ~ ind60
dem65 ~ ind60 + dem60
# residual covariances
y1 =~ y5
y2 =~ y4 + y6
y3 =~ y7
y4 =~ y8
y6 =~ y8
'

fit <- sem(model, data=PoliticalDemocracy)
summary(fit)
```

4. AMOS





Types of SEM

1. Covariance Based SEM or CB-SEM

- ✓ CB-SEM is a covariance-based SEM applied to confirm or reject the already existing theories.

2. Partial Least Square SEM or PLS-SEM

- ✓ PLS-SEM is a variance-based SEM applied to propose new theories and added new facts and information to the research field (Hair et al., 2011).



Model Development

- ✓ A conceptual model is developed on the basis of relevant theory .
- ✓ Formulation of hypotheses to test the causal relationships among latent constructs and observed variables, which were also called as indicators.



Elements of SEM

- ✓ SEM is classified into two vital elements viz. Measurement Model Assessment and Structural Model Assessment.

I. Measurement Model Assessment

- ✓ Measurement Model is also called as CFA.
- ✓ It specifies relationships between indicators and constructs.
- ✓ Measurement Model explains how the latent constructs could be measured.

✓ Assessment of Measurement Model is accomplished by establishing constructs' Reliability and Validity.

1. Reliability of the Constructs:

- ✓ Reliability measures the extent to which a test actually measures what it is expected to measure.
- ✓ It included assessment of internal consistency which was measured through Composite Reliability (*Lin and Ding, 2006*), Indicator Reliability (outer loadings).
- ✓ Composite Reliability (CR) > 0.7 (*Hair et al., 1998; Fornell & Larcker, 1981*)
- ✓ Cronbach's α (CA) > 0.7 (*Nunnally & Bernstein, 1994*)



2. Validity of the Constructs: Refers to the ability of a research instrument to measure what it is designed to measure.

✓ Measured through Convergent Validity & Discriminant Validity (*Hair et al., 1998; Bagozzi and Edwards, 1998*)

a. Convergent Validity: Represents the degree up to which a measure correlates positively with other measures of the same construct. Recommended values for Convergent Validity are:

Factor loadings > 0.7 , AVE > 0.5

(*Hair et al., 2010*)



b. Discriminant validity: The extent to which a construct is truly distinct from other constructs by empirical standards.

- ✓ Discriminant Validity can also be assessed through Fornell-Larcker Criterion (Hair et al., 2010).
- ✓ According to this criterion, Square-root of AVE should be greater than the Inter-Construct Correlation.
- ✓ Discriminant Validity can also be assessed through Cross Loadings i.e the loadings which it calculated on other constructs.



II. Structural Model Assessment

1. Assessment of collinearity issues of Structural Model

✓ The structural model is specified after assessing the validity and reliability of the reflective model through a measurement model.

a. Variance Inflation Factor (*Kline, 1998*)

$VIF < 5$ (*Grewal et al., 2004; Hair et al., 2011*), ,

$$VIF = 1 / \text{Tolerance}$$



b. Tolerance Value

- ✓ Tolerance Value is an indicator of how much of the variability of an independent variable is not explained by other independent variable in the model.
- ✓ Tolerance level > 0.2 (Hair et al., 2010).
- ✓ *Tolerance Value = $1 - R^2$ for each variable*



2. Hypotheses Testing

- ✓ Standardized Path coefficients (β) of the structural model represent the magnitude and direction of relationships and were thus used for Hypotheses Testing
- ✓ t-statistics (>1.96) and significance levels at $p < 0.05$.



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Any Questions ??



Thank You